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## Exploring microstructures of metal-doped oxides via simulated Raman spectrum

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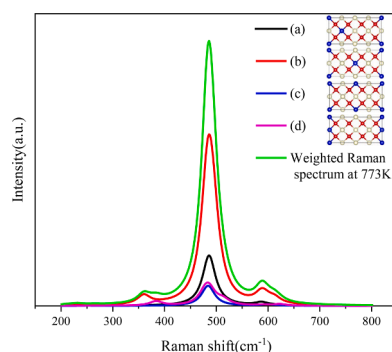
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### HIGHLIGHTS

- Global searching, Boltzmann distribution and Raman simulation was integrated.
- Weighted Raman spectra of Zr-doped ceria was used as a demonstration.
- It is also validated for analysis of microstructure of metal composite oxides.
- This provides a solution to explore the microstructure of composites.

### GRAPHICAL ABSTRACT



### ARTICLE INFO

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Microstructure

### ABSTRACT

Solid solution of metal-doped oxide has been widely used in material industry and catalysis process. Its performance is highly correlated with the distribution of doped ions. Due to the complex distribution of doped ions in solid solution and its variation with temperatures, to obtain the microstructures of metal-doped ions in solid solution remains a substantial challenge. Taken  $Ce_{1-x}Zr_xO_2$  as a model, the global structure searching, structures proportion with temperature determined by Boltzmann distribution, and the weighted simulation Raman spectra were integrated to explore the microstructures of metal-doped solid solution oxides. It was further verified by application into rutile and anatase  $TiO_2$  mixture, indicating that the present method is feasible to deduce the microstructure of metal composite oxides. We anticipate that it provides a powerful solution to explore microstructures of solid solution and complex metal oxides.

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## 1. Introduction

Solid solution of metal-doped oxide is a very important kind of metal composite oxides and has been widely used in material industry and catalysis process [1–5]. By introducing the doped ions to form new chemical bonds, the thermal and chemical stability, as well as performances could be enhanced [6–8]. For example, Li et al. [9] studied the iron-doped ceria and found that Ce-Fe-O solid solution forms when the concentration of iron ion is less than 0.3; while Fe<sub>2</sub>O<sub>3</sub> appears with further increase of the concentration of Fe ion with higher activity in CH<sub>4</sub> oxidation. Sartoretti et al. [10] investigated Cu and Mn-doped ceria and found that 5 % Cu-doped catalyst has higher surface area, but lower activity in soot oxidation; while 5 % Mn-doped ceria has the best activity in soot oxidation. Therefore, the catalytic performance of metal-doped solid solution is closely related to the type, concentration and distribution of doping ions [11].

Compared with the type and concentration of doping ions, the distribution of doped ions in solid solution also plays a key role in oxidative catalysis. It was reported that the metal-doped oxides mostly follow the Mars-van Krevelen mechanism, in which the doped ions integrate into the lattice of catalyst and lead to the geometrical stress and charge imbalance [12]. Hence, metal-doped oxides usually have lower oxygen defect formation energy and generate more oxygen vacancies than pure oxides due to the doped ion radius and charge imbalance [13]. Correspondingly, O<sub>2</sub> adsorbs on oxygen defects and forms active oxygen species to participate in the oxidation reaction [14]. Therefore, the catalytic performances of metal-doped oxides are highly correlated with the formation energy of oxygen defects, which in turn is closely related to the distribution of doped ions [15]. This is due to the fact that the oxygen defect formation energy in pure metal oxide only depends on the interaction between the host metal (M1) ions and oxygen atoms (M1-O-M1); while in solid solution with doped metal ion (M2), there are M1-O-M1, M1-O-M2 and M2-O-M2 interactions depending on the distribution of the doped metal ions in solid solution [16]. Therefore, exploring the corresponding distribution would improve the understanding of the microstructure of the doped solid solution and help the rational design and development of metal-doped oxides with high performance.

However, due to the complex distribution of doped ions in solid solution and variation with temperature, obtaining the microstructure information remains a substantial challenge. Among the widely used characterization techniques, X-ray diffraction (XRD) can determine whether solid solution is formed or not by measuring lattice parameters of doped solid solution [17]; X-ray photoelectronic spectroscopy (XPS) can measure the valence of elements in surface layer of materials [18]; X-ray fluorescence spectroscopy (XRF) can measure the concentration of atoms in composite oxides; UV-Vis can determine whether there are isolated doped cations; EXAFS can measure the coordination environment and structure of doped atoms [19]. Although these techniques greatly enriched our knowledge on the microstructure of metal doped solid solution, they are hard to obtain the quantitative distribution of metal-doped oxides.

Raman spectroscopy is a rapid nondestructive technology [20], which can provide important structure information by measuring the characteristic vibration of pure and doped phase [21–26]. For example, Ce<sub>1-x</sub>Zr<sub>x</sub>O<sub>2</sub> (0 < x < 0.5) is a typical solid solution with a high Raman peak of 485 cm<sup>-1</sup>, as well as a wide and small peak of 600 cm<sup>-1</sup> [27]. Using the most stable Ce<sub>6</sub>Zr<sub>2</sub>O<sub>8</sub> model, our simulated Raman spectrum indicated that the 485 cm<sup>-1</sup> peak is contributed by F<sub>2g</sub> vibration; and the wide and small one of 600 cm<sup>-1</sup> is designated to Ce<sup>4+</sup>-O-Zr<sup>4+</sup> vibration [28]. Furthermore, the F<sub>2g</sub> peak of Ce<sub>1-x</sub>Zr<sub>x</sub>O<sub>2</sub> solid solution blue shifts about 25 cm<sup>-1</sup> compared with 460 cm<sup>-1</sup> of CeO<sub>2</sub>, which is derived from the relatively smaller size of Zr<sup>4+</sup> ion (0.84 Å) compared with Ce<sup>4+</sup> ion (0.97 Å). Although the simulated spectrum interpreted the derivation of Raman peaks of Ce<sub>1-x</sub>Zr<sub>x</sub>O<sub>2</sub> solid solution at a molecular level, the narrow peak at 600 cm<sup>-1</sup> of the simulated spectrum is quite different from the small and wide peak in experimental spectrum. This might be

attributed to the various Ce and Zr distributions in Ce<sub>1-x</sub>Zr<sub>x</sub>O<sub>2</sub> solid solution, which cannot be represented by the most stable structure. Therefore, it is possible to obtain a spectrum close to the experimental one if the composition of solid solution approaches the practical catalyst. Correspondingly, the Ce and Zr distribution in metal-doped oxides can be reasonably obtained by simulated Raman spectra.

To solve the challenge of the microstructures of doped ions in solid solution, using Ce<sub>1-x</sub>Zr<sub>x</sub>O<sub>2</sub> as a case, a protocol to quantitatively determine the microstructures of doped ions was proposed to get the weighted theoretical Raman spectrum in the present work based on Boltzmann statistical average of different configurations [29–31]. It was further verified by application in mixed TiO<sub>2</sub> by correlating the ratio of mixed oxides with the simulated Raman spectra. Therefore, it provides a feasible solution to establish the possible relationship between the material structure and Raman spectra.

## 2. Method and models

The present protocol includes the global searching and optimization of the possible structures of solid solution oxide, simulation of Raman spectra of different configurations, as well as calculation of the weighted theoretical Raman spectrum. For clear explanation, the solid solution of Ce<sub>1-x</sub>Zr<sub>x</sub>O<sub>2</sub> which has been widely applied in the elimination of volatile organic compounds, the three-way catalytic purification of automobile exhaust, etc., was taken as an example [32,33]. A supercell of Ce<sub>6</sub>Zr<sub>2</sub>O<sub>16</sub> was adopted to represent the Ce<sub>0.75</sub>Zr<sub>0.25</sub>O<sub>2</sub> solid solution, and all of its possible structures were generated by using the site-occupancy disorder (SOD) method [34], in which all the possible configurations was generated by atomic substitutions via the group of symmetry operator in parent structure. Then the structures were optimized by Vienna ab initio simulation package (VASP) [35]. Projector augmented wave (PAW) [36] pseudopotential was utilized with Perdew-Burke-Ernzerhof [37] functional and generalized gradient approximation. Monkhorst-Pack method was adopted for Brillouin zone sampling [38]. Kohn-Sham equations were solved with a cutoff energy of 400 eV. 1.0 × 10<sup>-8</sup> eV and 0.01 eV/Å were set for the energy convergence criterion and the maximum Hellmann-Feynman force, respectively [23]. DFT + *U* method with *U* value of 5 eV for Ce atom was performed for the correction of on-site Coulombic and exchange interactions produced by strong localization of 4*f* electrons [39,40]. The Raman spectrum simulation includes the matrix vibration calculation phonon spectra and dielectric coefficient by density functional perturbation theory (DFPT) [41–43].

The proportion of Ce<sub>6</sub>Zr<sub>2</sub>O<sub>16</sub> with different structures in solid solution at specific temperature was calculated based on the equation of Boltzmann distribution, Eq. (1) [44].

$$\frac{N_i}{N} = \frac{g_i e^{-\frac{(\Delta\epsilon_i + \epsilon_{\text{Ref}})}{kT}}}{\sum_j g_j e^{-\frac{(\Delta\epsilon_j + \epsilon_{\text{Ref}})}{kT}}} = \frac{g_i e^{-\frac{\Delta\epsilon_i}{kT}}}{\sum_j g_j e^{-\frac{\Delta\epsilon_j}{kT}}} \quad (1)$$

where  $N_i$  is the number of *i*th structure;  $N$  is the total number of all structures;  $g_i$  is degeneracy of *i*th structure;  $\epsilon_{\text{Ref}}$  is the free energy of the most stable configuration;  $\Delta\epsilon_i$  is the free energy difference of *i*th structure compared with  $\epsilon_{\text{Ref}}$ ;  $k$  is Boltzmann's constant.

The weighted simulation Raman spectra was calculated according to the following equation.

$$I_{\text{total}} = \sum_i \left( \frac{N_i}{N} \times I_i \right) \quad (2)$$

where  $I_i$  and  $I_{\text{total}}$  are the intensities of Raman spectra for the *i*th structure and the total one, respectively.  $N_i/N$  is the structural proportion of the *i*th configuration.

### 3. Results and discussion

After the global searching and optimization of the supercell of  $\text{Ce}_6\text{Zr}_2\text{O}_{16}$  by SOD method and DFT calculation, four stable configurations and their simulated Raman spectra were depicted in Fig. 1; the free energies and proportion at different temperature based on the Boltzmann distribution calculation were listed in Table 1.

As listed in Table 1, Structure (a) with the biggest distance of two Zr ions is the most stable configuration and is dominant in solid solution at zero temperature. When the temperature increases to 300 K, the ratios of Structure (a)~(d) are 0.279, 0.677, 0.023 and 0.020, respectively. With further increase to 773 K, the ratios of Structure (a) and (b) decrease to 0.190 and 0.646, respectively; while the ratio of Structure (c) and (d) increase to 0.076 and 0.088, respectively. Therefore, it can be reasonably deduced that the Raman spectra of  $\text{Ce}_{1-x}\text{Zr}_x\text{O}_2$  will vary with temperature.

Fig. 1 showed that the  $F_{2g}$  vibration modes of all configurations blue shift to  $485\text{ cm}^{-1}$  compared with  $\text{CeO}_2$  ( $460\text{ cm}^{-1}$ ) due to the lattice contraction and the shortening of Ce-O bond length caused by the doping Zr ions [25]. The Raman spectra of Structure (a) and (c) are very similar since the  $F_{2g}$  peaks almost overlap, and there is only one small peak at  $585$  (a) and  $600\text{ cm}^{-1}$  (c), which are assigned as  $\text{Zr}^{4+}\text{-O-Ce}^{4+}$  vibration peak. Except for the  $F_{2g}$  peak, Structure (b) has three peaks at  $360$ ,  $589$  and  $610\text{ cm}^{-1}$ , which are caused by vibrations of  $\text{O-Zr}^{4+}\text{-O}$ ,  $\text{Zr}^{4+}\text{-O-Ce}^{4+}$  and  $\text{Zr}^{4+}\text{-O-Zr}^{4+}$ , respectively. The Raman spectrum of Structure (d) is similar to that of Structure (b) with two small peaks at  $590$  and  $622\text{ cm}^{-1}$ , respectively. The calculation results above indicated that a small and wide Raman peak may appear from  $580\text{ cm}^{-1}$  to  $630\text{ cm}^{-1}$  due to the coexistence of multiple microstructures of  $\text{Ce}_{1-x}\text{Zr}_x\text{O}_2$  solid solution.

To verify the theoretical deduction of the weak broad peaks between  $580$  and  $620\text{ cm}^{-1}$  derived from the overlap of  $\text{Ce}_{1-x}\text{Zr}_x\text{O}_2$  with different Ce and Zr distribution, the weighted Raman spectra at different temperature were calculated and shown in Fig. 2. At 0 K, the Raman spectrum of  $\text{Ce}_{1-x}\text{Zr}_x\text{O}_2$  is determined by the most stable Structure (a) with a  $F_{2g}$  peak of  $485\text{ cm}^{-1}$  and a characteristic one of  $586\text{ cm}^{-1}$ . When temperature rises to 300 K, the fractions of Structure (a)~(d) are 0.279, 0.677, 0.023 and 0.020, respectively. Hence, the weighted Raman spectrum at 300 K is mainly contributed by Structure (a) and (b). When temperature is up to 773 K, the ratios of Structure (a)~(d) are 0.190, 0.646, 0.076 and 0.088. Corresponding, the small and broad Raman peaks at  $580\sim 630\text{ cm}^{-1}$  are contributed by all the four structures. The small and broad peak between  $585\text{ cm}^{-1}$  and  $620\text{ cm}^{-1}$  are derived from vibrations of  $\text{Zr}^{4+}\text{-O-Ce}^{4+}$  and  $\text{Zr}^{4+}\text{-O-Zr}^{4+}$  of  $\text{Ce}_{1-x}\text{Zr}_x\text{O}_2$  solid solution with different Ce and Zr distribution, respectively. The peak of  $585\text{ cm}^{-1}$

is mainly caused by the  $\text{Zr}^{4+}\text{-O-Ce}^{4+}$  vibration; and the peak of  $620\text{ cm}^{-1}$  is caused by  $\text{Zr}^{4+}\text{-O-Zr}^{4+}$  vibration. Their overlap results in the broadening of Raman peak of  $580\sim 630\text{ cm}^{-1}$ . Fig. 2 also indicates that the peaks at  $580\sim 630\text{ cm}^{-1}$  blue shift with the increase of temperature, indicating the microstructure varies with temperature.

To prove this deduction above, the  $\text{Ce}_{0.75}\text{Zr}_{0.25}\text{O}_2$  samples were prepared by the citrate sol-gel method and treated with two heated approaches. One was calcined at 773 K for 4 h and slowly annealed at muffle furnace to room temperature; the other one was calcined at 773 K for 4 h and fast cooled to room temperature. As shown in Fig. 3, the inset of X-ray diffraction patterns showed that  $\text{Ce}_{0.75}\text{Zr}_{0.25}\text{O}_2$  solid solution forms without  $\text{CeO}_2$  or  $\text{ZrO}_2$  segregation; and the characteristic peak derived from the  $\text{Zr}^{4+}\text{-O-Ce}^{4+}$  and  $\text{Zr}^{4+}\text{-O-Zr}^{4+}$  vibrations blue shifts to  $607\text{ cm}^{-1}$  for the quick cooling sample compared with the annealed sample ( $599\text{ cm}^{-1}$ ). This is attributed to the fact that the diverse Ce and Zr distribution at high temperature was retained due to the quick cooling, which leads to the higher ratio of Structure (d) in  $\text{Ce}_{0.75}\text{Zr}_{0.25}\text{O}_2$  than the annealed sample. Therefore, the vibration signal of  $\text{Zr}^{4+}\text{-O-Zr}^{4+}$  in Raman spectrum increases, which leads to the blueshift and broadening of the characteristic peak at  $580\sim 630\text{ cm}^{-1}$ . For the samples annealed for 4 h, the structural stress is eliminated upon annealing and leads to a higher ratio of Structure (a). Hence its vibration peak of  $\text{Zr}^{4+}\text{-O-Ce}^{4+}$  is relatively high, which is well consistent with the theoretical deduction. Therefore, it is feasible to deduce the structural information of metal composite oxides by combining the experimental Raman spectra and simulated spectra.

To demonstrate the feasibility of the present method, rutile and anatase  $\text{TiO}_2$  which have been widely applied in photocatalysis were adopted [45–48]; and their Raman spectra, as well as mixture (53.4 % rutile and 46.6 % anatase) were calculated and shown in Fig. 4. Fig. 4(a) shows that the Raman peaks of  $B_{1g}$ ,  $E_g$ ,  $A_{1g}$  and  $B_{2g}$  vibration modes are at  $182$ ,  $462$ ,  $606$  and  $714\text{ cm}^{-1}$ , respectively, which are in good accordance with the experimental results. Meanwhile, as depicted in Fig. 4(b), the  $E_g$  peaks of anatase  $\text{TiO}_2$  correspond to  $168$  and  $642\text{ cm}^{-1}$ ; the  $B_{1g}$  peaks are at  $378$  and  $493\text{ cm}^{-1}$ ; the  $A_{1g}$  peak is at  $513\text{ cm}^{-1}$ , which also agree with experimental results [49].

On the basis of the experimental ratio of rutile (0.534) and anatase (0.466)  $\text{TiO}_2$ , the weighted Raman spectrum was calculated. Fig. 4(a) shows that the peak at  $168\text{ cm}^{-1}$  is derived from the overlap of the  $B_{1g}$  mode of rutile and  $E_g$  mode of anatase  $\text{TiO}_2$ ; the peaks at  $350\sim 550\text{ cm}^{-1}$  are contributed by the  $E_g$ ,  $B_{1g}$  and  $A_{1g}$  modes of rutile and anatase  $\text{TiO}_2$ , respectively; the peaks at  $606$  and  $642\text{ cm}^{-1}$  are attributed to the  $A_{1g}$  of rutile and  $E_g$  of anatase  $\text{TiO}_2$ , respectively. These results indicate that the weighted simulated Raman spectrum of  $\text{TiO}_2$  mixture is well consistent with the experimental results [46]. Therefore, the practical spectrum of composite oxide is derived from the overlap of Raman spectra with different structures, and the weighted simulation Raman spectra can provide important structural information of metal composite oxides.

### 4. Conclusion

In summary, to solve the challenge of the microstructures of composite oxide, global structure optimization, structure proportion with temperature determined by Boltzmann distribution, and the weighted simulation Raman Spectrum was integrated. It follows the steps: (1) Optimization of the possible structures with different microstructures; (2) Calculation of the proportions of different structures by Boltzmann distribution law; (3) Simulation of Raman spectra of different structures by DFPT theory; (4) Computation of the weighted Raman spectrum on the basis of the proportion of different structures. Using  $\text{Ce}_x\text{Zr}_{1-x}\text{O}_2$  as a model, the microstructure of Ce and Zr distribution in  $\text{Ce}_{1-x}\text{Zr}_x\text{O}_2$  solution at different temperature can be determined by combining with the experimental and simulated Raman spectra. It is further validated by rutile and anatase  $\text{TiO}_2$  mixture. We anticipate that the present method provides an effective solution and a powerful tool for exploring the

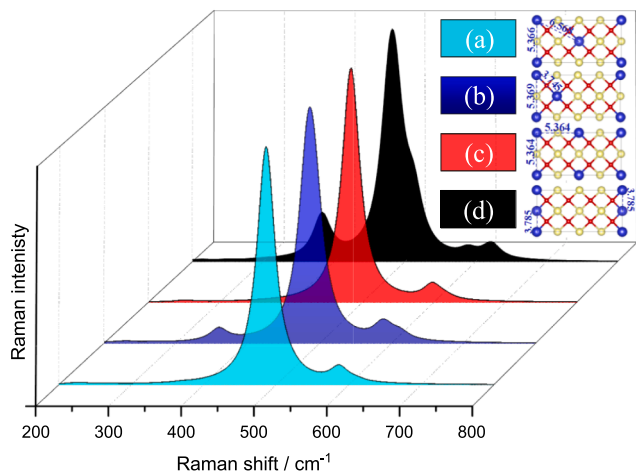
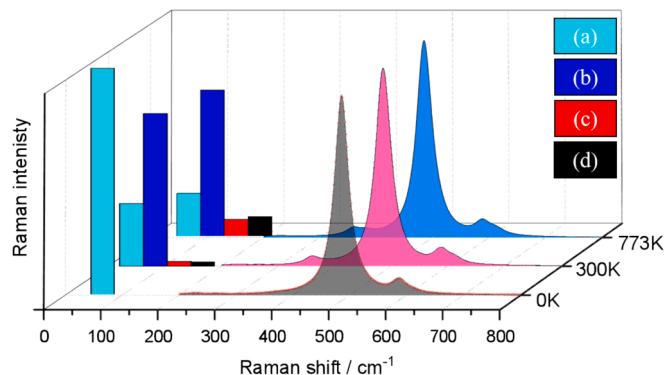


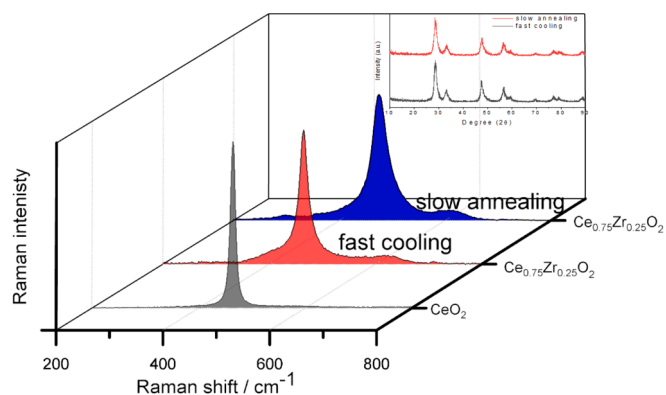
Fig. 1. Simulated Raman spectra of four  $\text{Ce}_6\text{Zr}_2\text{O}_{16}$  configurations with different Zr-Zr distance.

**Table 1**  
Free energy and population of the possible  $\text{Ce}_6\text{Zr}_2\text{O}_{16}$  configurations.

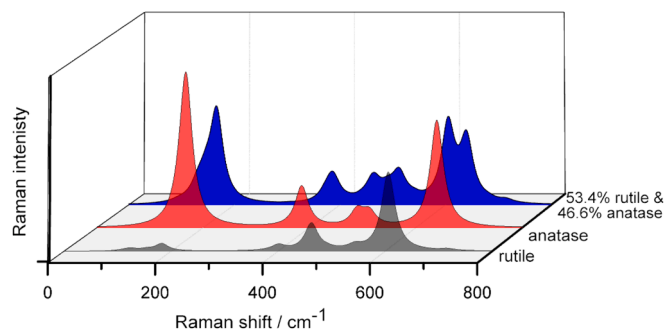
Structure	Degeneracy	$G_0$ / eV mol <sup>-1</sup>	Population at 0 K	$G_{300\text{ K}}$ / eV mol <sup>-1</sup>	Population at 300 K	$G_{773\text{ K}}$ / eV mol <sup>-1</sup>	Population at 773 K
(a)	4	-201.470	1.00	-201.809	0.279	-203.704	0.190
(b)	16	-201.455	0	-201.796	0.677	-203.693	0.646
(c)	4	-201.401	0	-201.744	0.023	-203.643	0.076
(d)	4	-201.388	0	-201.741	0.020	-203.652	0.088



**Fig. 2.** Weighted Raman spectra at different temperatures.



**Fig. 3.** Raman spectra of  $\text{Ce}_{0.75}\text{Zr}_{0.25}\text{O}_2$  samples calcined at 773 K for 4 h. The inset is XRD patterns of  $\text{Ce}_{0.75}\text{Zr}_{0.25}\text{O}_2$  solid solution with slow annealing (redline) and fast cooling (black line).



**Fig. 4.** Simulated Raman spectra of rutile (a) and anatase (b)  $\text{TiO}_2$ .

microstructure of composites.

#### CRediT authorship contribution statement

Le Liu: Writing – original draft, Investigation, Formal analysis. Yuxing Xu: Validation, Investigation, Funding acquisition. Junchao

Su: Formal analysis. Jiangtao Wei: Formal analysis. Xingchen Liu: Writing – review & editing, Formal analysis. Qing Peng: Writing – review & editing, Formal analysis, Conceptualization. Jie Chang: Writing – review & editing, Formal analysis, Conceptualization. Botao Teng: Writing – review & editing, Supervision, Project administration, Funding acquisition, Conceptualization.

#### Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

#### Data availability

The data that support the findings of this study are available from the corresponding author upon reasonable request.

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#### Appendix A. Supplementary data

Supplementary data to this article can be found online at <https://doi.org/10.1016/j.saa.2024.124616>.

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